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**"Why did Jimmy do well on the Math test after drinking orange juice?"**

On #1-11, simplify each expression, then on #12-17 solve each equation. The answer to each problem will match a letter that will allow you to figure out the joke.

**Simplify.**

1.  $\sqrt{-49}$

2.  $-\sqrt{-100}$

3.  $3\sqrt{-18}$

4.  $-5\sqrt{-9}$

5.  $3 + \sqrt{-25}$

6.  $(3 + 2i) + (2 + 7i)$

7.  $(4 - 5i) - (-10 + 3i)$

8.  $2(3 + 6i) - 3(7 - 5i)$

9.  $(2 + \sqrt{-25}) + (-8 - \sqrt{-9})$

10.  $(3 - 5\sqrt{-7}) - (4 + 3\sqrt{-7})$

11.  $(2 - 7\sqrt{-18}) + (-3 + 4\sqrt{-50})$

**Solve.**

12.  $x^2 = -81$

13.  $x^2 = -2$

14.  $x^2 + 49 = 0$

15.  $x^2 + 50 = 2$

16.  $3x^2 + 12 = x^2 - 20$

17.  $5(x^2 - 4) = 3(2x^2 + 6)$

14 - 8i	-10i	$\pm 9i$	$-15 + 27i$	$\pm 4i$	-15i	$3 + 5i$	$-1 - i\sqrt{2}$	$\pm 7i$
E	E	R	S	W	n	A	T	D
$\pm i\sqrt{2}$	$9i\sqrt{2}$	$-1 - 8i\sqrt{7}$	$7i$	$\pm i\sqrt{38}$	$-6 + 2i$	$\pm 4i\sqrt{3}$	$5 + 9i$	
H	T	C	n	A	E	C	O	

13    2    16    5    8    10    6    4    15    9    1    11    12    17    3    7    14

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