# Mathematics Station Activities

# for Common Core State Standards Grade 8







# **Table of Contents**

Standards Correlations	v
Introduction	
Materials List	x
The Number System	1
Set 1: Radicals and Irrational Numbers	1
Set 2: Rational and Irrational Numbers	
Set 3: Using Rational Approximations of Irrational Numbers	16
Expressions and Equations	
Set 1: Problem Solving with Exponents and Scientific Notation	
Set 2: Graphing Linear Equations/Solving Using Graphs	31
Set 3: Writing Linear Equations	48
Set 4: Solving 2-by-2 Systems by Graphing	56
Set 5: Solving 2-by-2 Systems by Substitution	67
Set 6: Solving 2-by-2 Systems by Elimination	77
Functions	88
Set 1: Real-World Situation Graphs	88
Set 2: Relation vs. Function and Linear vs. Nonlinear	101
Set 3: Slope and Slope-Intercept Form	114
Geometry	124
Set 1: Transformations	124
Set 2: Translations and Rotations	133
Set 3: Properties of Angle Pairs	140
Set 4: Properties of Lines Cut by Transversals	147
Set 5: Properties of Right Triangles	154
Set 6: Understanding the Pythagorean Theorem	161
Set 7: Volume of Cylinders, Cones, and Spheres	168
Statistics and Probability	177
Set 1: Data and Relationships	177
Set 2: Scatter Plots	189

Station Activities for Common Core Mathematics, Grade 8

iii

# **Standards Correlations**

The standards correlations below support the implementation of the Common Core Standards. This book includes station activity sets for the Common Core domains of The Number System; Expressions and Equations; Functions; Geometry; and Statistics and Probability. The following table provides a listing of the available station activities organized by Common Core standard.

The left column lists the standard codes. The first number of the code represents the grade level. The grade number is followed by the initials of the Common Core domain name, which is then followed by the standard number. The middle column of the table lists the title of the station activity set that corresponds to the standard(s), and the right column lists the page number where the station activity set can be found.

Standard	Set title	Page number
8.NS.1.	Radicals and Irrational Numbers	1
8.NS.1.	Rational and Irrational Numbers	9
8.NS.2.	Using Rational Approximations of Irrational Numbers	16
8.EE.1.	Problem Solving with Exponents and Scientific Notation	24
8.EE.2.	Rational and Irrational Numbers	9
8.EE.3.	Problem Solving with Exponents and Scientific Notation	24
8.EE.4.	Problem Solving with Exponents and Scientific Notation	24
8.EE.5.	Graphing Linear Equations/Solving Using Graphs	31
8.EE.5.	Writing Linear Equations	48
8.EE.8.	Solving 2-by-2 Systems by Graphing	56
8.EE.8.	Solving 2-by-2 Systems by Substitution	67
8.EE.8.	Solving 2-by-2 Systems by Elimination	77
8.F.1.	Slope and Slope-Intercept Form	114
8.F.3.	Relation vs. Function and Linear vs. Nonlinear	101
8.F.5.	Real-World Situation Graphs	88
8.G.1.	Transformations	124

(continued)

# **Standards Correlations**

Standard	Set title	Page number
8.G.1.	Translations and Rotations	133
8.G.2.	Translations and Rotations	133
8.G.3.	Transformations	124
8.G.3.	Translations and Rotations	133
8.G.5.	Properties of Angle Pairs	140
8.G.5.	Properties of Lines Cut by Transversals	147
8.G.6.	Properties of Right Triangles	154
8.G.6.	Understanding the Pythagorean Theorem	161
8.G.7.	Understanding the Pythagorean Theorem	161
8.G.7.	Properties of Right Triangles	154
8.G.8.	Properties of Right Triangles	154
8.G.8.	Understanding the Pythagorean Theorem	161
8.G.9.	Volume of Cylinders, Cones, and Spheres	168
8.SP.1.	Data and Relationships	177
8.SP.1.	Scatter Plots	189
8.SP.2.	Scatter Plots	189
8.SP.2.	Data and Relationships	177
8.SP.4.	Data and Relationships	177
8.SP.4.	Scatter Plots	189

Station Activities for Common Core Mathematics, Grade 8

Set 1: Radicals and Irrational Numbers

### Instruction

Goal: To provide opportunities for students to develop concepts and skills related to simplifying radicals, performing operations with radicals, and classifying and comparing rational versus irrational numbers

#### **Common Core Standards**

#### The Number System

Know that there are numbers that are not rational, and approximate them by rational numbers.

**8.NS.1.** Know that numbers that are not rational are called irrational. Understand informally that every number has a decimal expansion; for rational numbers show that the decimal expansion repeats eventually, and convert a decimal expansion, which repeats eventually into a rational number.

# Student Activities Overview and Answer Key

#### Station 1

Students are given 18 small, equal-sized algebra square tiles. Students work together to simplify radicals by factoring out a perfect square, using the algebra tiles as a visual reference. Students show two different ways to simplify a given radical by factoring out perfect squares.

#### Answers

- 1.  $\sqrt{4}$ ; 4;  $\sqrt{4 \cdot 2}$ ;  $2\sqrt{2}$ 2.  $\sqrt{12}$ ; 4;  $\sqrt{4 \cdot 3}$ ;  $2\sqrt{3}$
- 2.  $\sqrt{12}$ ; 4;  $\sqrt{4} \bullet 3$ ;  $2\sqrt{3}$
- 3.  $\sqrt{18}$ ; 9;  $\sqrt{9 \cdot 2}$ ;  $3\sqrt{2}$
- 4.  $\sqrt{48} = \sqrt{16 \cdot 3} = 4\sqrt{3}$  and  $\sqrt{48} = \sqrt{12 \cdot 4} = 2\sqrt{12} = 2\sqrt{4 \cdot 3} = 4\sqrt{3}$

#### Station 2

Students are given 12 index cards with the following numbers written on them:

$$-25\sqrt{12}, 3\sqrt{12}, -8\sqrt{3}, \sqrt{3}, 10\sqrt{7}, 12\sqrt{10}, -4\sqrt{10}, 100\sqrt{10},$$
  
 $12\sqrt{15}, -20\sqrt{15}, 15\sqrt{21}, 21\sqrt{21}$ 

The index cards will be shuffled. One student will deal each student an equal number of cards (i.e., if there are four students, then each student will receive three cards). Each student will place one of their cards in the center of the table. Students will work together to determine which radicals can be added together or subtracted.

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Station Activities for Common Core Mathematics, Grade 8

Set 1: Radicals and Irrational Numbers

#### Instruction

#### Answers

- 1. Answers will vary. Possible answers:  $-25\sqrt{12} + 3\sqrt{12} = -22\sqrt{12}$  and  $-25\sqrt{12} - 3\sqrt{12} = -28\sqrt{12}$  OR  $3\sqrt{12} - (-25\sqrt{12}) = 28\sqrt{12}$
- 2. Answers will vary. Possible answers:  $12\sqrt{10} + 100\sqrt{10} = 112\sqrt{10}$  and  $12\sqrt{10} - 100\sqrt{10} = -88\sqrt{10}$  OR  $100\sqrt{10} - 12\sqrt{10} = 88\sqrt{10}$
- 3. Answers will vary. Possible answers:  $15\sqrt{21} + 21\sqrt{21} = 36\sqrt{21}$  and  $15\sqrt{21} - 21\sqrt{21} = -6\sqrt{21}$  OR  $21\sqrt{21} - 6\sqrt{21} = 15\sqrt{21}$
- 4. The radicands have to be equal.

#### **Station 3**

Students are given 12 index cards with the following numbers written on them:

 $5\sqrt{12}$ ,  $3\sqrt{4}$ ,  $-8\sqrt{15}$ ,  $6\sqrt{6}$ ,  $12\sqrt{10}$ ,  $-4\sqrt{10}$ ,  $7\sqrt{2}$ ,  $8\sqrt{20}$ ,  $12\sqrt{10}$ ,  $15\sqrt{20}$ ,  $3\sqrt{5}$ ,  $\sqrt{30}$ 

Students will draw two cards at a time from the pile of index cards. They will work together to multiply and divide the radicals on the index cards and record their answers in a table.

#### Answers

Answers will vary. Possible answers:

Index card #1	Index card #2	Multiplication	Division
$5\sqrt{12}$	$3\sqrt{4}$	$15\sqrt{48} = 60\sqrt{3}$	$\frac{5\sqrt{12}}{3\sqrt{4}} = \frac{5\sqrt{3}}{3}$
$6\sqrt{6}$	$-4\sqrt{10}$	$-24\sqrt{60} = -48\sqrt{15}$	$\frac{6\sqrt{6}}{-4\sqrt{10}} = \frac{3\sqrt{3}}{-2\sqrt{5}}$

## Instruction

#### **Station 4**

Students use two number cubes to generate two numbers. They work together to arrange the two numbers as a rational number and an irrational number. Students give their reasoning behind creating rational and irrational numbers for the same two numbers.

#### Answers

1–4. Answers will vary.

#### **Materials List/Setup**

Station 1	18 small, equal-sized algebra square tiles			
Station 2	12 index cards with the following numbers written on them:			
	$-25\sqrt{12}, 3\sqrt{12}, -8\sqrt{3}, \sqrt{3}, 10\sqrt{7}, 12\sqrt{10}, -4\sqrt{10},$			
	$100\sqrt{10}$ , $12\sqrt{15}$ , $-20\sqrt{15}$ , $15\sqrt{21}$ , $21\sqrt{21}$			
Station 3	12 index cards with the following numbers written on them:			
	$5\sqrt{12}$ , $3\sqrt{4}$ , $-8\sqrt{15}$ , $6\sqrt{6}$ , $12\sqrt{10}$ , $-4\sqrt{10}$ ,			
	$7\sqrt{2}, 8\sqrt{20}, 12\sqrt{10}, 15\sqrt{20}, 3\sqrt{5}, \sqrt{30}$			

**Station 4** two number cubes

3

#### Instruction

#### **Discussion Guide**

To support students in reflecting on the activities and to gather formative information about student learning, use the following prompts to facilitate a class discussion to "debrief" the station activities.

#### **Prompts/Questions**

- 1. How do you simplify radicals using a perfect square?
- 2. Provide three real-world examples of when you would use and simplify radicals.
- 3. What has to be equal in order to add and subtract radical numbers? What is this quantity called?
- 4. How do you add and subtract radical numbers?
- 5. How do you multiply and divide radical numbers?
- 6. How can you tell if a number is rational or irrational?

#### Think, Pair, Share

Have students jot down their own responses to questions, then discuss with a partner (who was not in their station group), and then discuss as a whole class.

#### **Suggested Appropriate Responses**

- 1. Factor out the perfect square and then take the square root of each number.
- 2. Answers may vary. Possible answers: Construction—using the Pythagorean theorem to construct triangular woodwork; Physics—using radicals in distance and acceleration equations; Finance—using radicals in calculations such as net present value.
- 3. The quantity under the radical sign is known as the radicand.
- 4. Add and/or subtract the numbers in front of the radical. Leave the radicand the same.
- 5. For multiplication, multiply the numbers in front of the radical. Multiply the radicands. For division, divide the numbers in front of the radical. Divide the radicands.
- 6. A rational number can be expressed exactly by a ratio of two integers. An irrational number cannot be expressed exactly by a ratio of two integers.

#### Possible Misunderstandings/Mistakes

- When a perfect square is identified, not taking the square root of the number before placing it in front of the radical
- Adding or subtracting radicals that do not have the same radicand
- Adding or subtracting the radicands
- Not multiplying or dividing the radicands in addition to multiplying and dividing the numbers in front of the radical

Set 1: Radicals and Irrational Numbers

#### Station 1

NAME:

You will be given 18 square algebra tiles and will need to simplify  $\sqrt{8}$ ,  $\sqrt{12}$ , and  $\sqrt{18}$ . Work together to create a group of 8 algebra tiles, factor out a perfect square, and simplify the radical. Repeat this process for a group of 12 algebra tiles and then 18 algebra tiles. Write your answers below.

1. Simplify  $\sqrt{8}$ .

What perfect square can you factor out of  $\sqrt{8}$ ? \_\_\_\_\_\_ Rewrite the original radical in factored form: \_\_\_\_\_\_ Find the square root of the perfect square and write your final answer for  $\sqrt{8}$ .

2. Simplify  $\sqrt{12}$ .

What perfect so	quare can you	ı factor out	of $\sqrt{12}$ ? _					
Rewrite the orig	ginal radical i	n factored	form:					
T' 1.1	( C.1	C ,	1 .	c c	1	C	10	

Find the square root of the perfect square and write your final answer for  $\sqrt{12}$  .

3. Simplify  $\sqrt{18}$ .

What perfect square can you factor out of  $\sqrt{18}$ ? \_\_\_\_\_\_ Rewrite the original radical in factored form: \_\_\_\_\_\_ Find the square root of the perfect square and write your final answer for  $\sqrt{18}$ .

4. In the space below, show two different ways to simplify  $\sqrt{48}$  by factoring out perfect squares.

Set 1: Radicals and Irrational Numbers

### Station 2

NAME:

You will be given 12 index cards with the following numbers written on them:

$$-25\sqrt{12}, \ 3\sqrt{12}, -8\sqrt{3}, \ \sqrt{3}, \ 10\sqrt{7}, \ 12\sqrt{10}, -4\sqrt{10}, \\ 100\sqrt{10}, \ 12\sqrt{15}, -20\sqrt{15}, \ 15\sqrt{21}, \ 21\sqrt{21}$$

Shuffle the index cards. Have one group member deal each of you an equal number of cards (i.e., if there are four students, then each one will receive three cards). Have each student place one of their cards in the center of the table. Work together to determine which radicals can be added together or subtracted. If none of the radicals can be added or subtracted, then place a round of new cards on the table. Repeat this process with your remaining cards. If time permits, reshuffle the cards and play again.

- 4. How did you know which radicals could be added or subtracted?

Set 1: Radicals and Irrational Numbers

#### Station 3

You will be given 12 index cards with the following numbers written on them:

$$5\sqrt{12}$$
,  $3\sqrt{4}$ ,  $-8\sqrt{15}$ ,  $6\sqrt{6}$ ,  $12\sqrt{10}$ ,  $-4\sqrt{10}$ ,  $7\sqrt{2}$ ,  $8\sqrt{20}$ ,  $12\sqrt{10}$ ,  $15\sqrt{20}$ ,  $3\sqrt{5}$ ,  $\sqrt{30}$ 

Place the index cards in a pile. Have one student draw two index cards. Work together to multiply and divide the radicals on the index cards. Repeat this process with your remaining cards. If time permits, reshuffle the cards and play again.

Record the index cards and your answers in the table below. Remember to simplify your answer.

Index card #1	Index card #2	Multiplication	Division

Station Activities for Common Core Mathematics, Grade 8

Set 1: Radicals and Irrational Numbers

#### Station 4

Use the two number cubes provided for problems 1–4.

1. Roll each number cube and record the results in the boxes below.



- 2. Work with other students to arrange these two numbers so they make up a rational number. Write your answer below. Give a reason for your answer.
- 3. Work with other students to arrange these two numbers so that they are irrational. Write your answer below. Give a reason for your answer.
- 4. Repeat the process three more times.





